

**PHY690J: Group Theory and its application to High Energy Physics**  
**Instructor: Joydeep Chakraborty**

**Topics**

1. Discrete and Continuous groups: very brief introduction.
2. Lie group :
  - (A) Character and Haar measure
  - (B) Young Tableaux
- (i) Compact connected groups:  $U(1)$ ,  $SU(N)$ ,  $Spin(2N)$ ,  $Spin(2N+1)$ ,  $Sp(2N)$
- (ii) Non-compact group: Lorentz group and its characters
3. Representation Theory:
  - (A) Roots, Weights, Cartan matrix, Dynkin diagrams
  - (B) Embeddings and Branching Rules.
  - (C) Gauge Theory
4. Invariant Polynomial construction: path to Lagrangian
5. Grand Unified Theory: through the eyes of representation theory
6. Spinors and helicity
7. Homotopy theories and topological defects.
8. Renormalization Groups and representation theories.
9. Anomalies in the context of Global and Gauge symmetries.

**Prerequisites**

Quantum Field Theory-I, Basic Mathematical Methods courses.

**References**

- (1) Rubakov: Classical Theory of Fields.
- (2) Dixon: A brief Introduction to Modern Amplitude Methods.
- (3) Slansky: Group Theory for unified model building.