

## SIMPLIFIED METHOD FOR PREDICTING AVERAGE SHEAR-WAVE VELOCITY OF GROUND AT STRONG-MOTION STATIONS

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### ABSTRACT :

We develop a method for estimating average shear-wave velocity in the upper 30 meters of the ground ( $V_{S30}$ ) at a strong-motion station by using recorded motions at a pair of stations located closely each other. For the station pair, an estimate of  $V_{S30}$  at one of the stations where the soil condition is unknown is derived mainly from  $V_{S30}$  at another station where the shear-wave velocity data is available and relative amplification factor between the stations. By applying this method to the ground motion records of the JMA, K-NET and KiK-net strong-motion networks in Japan, the  $V_{S30}$  values are estimated at 261 JMA strong-motion stations throughout Japan. The  $V_{S30}$  estimated in this study are compared with those inferred from boring data obtained in the vicinity of the JMA station. The result indicates that the method proposed in this study can predict the  $V_{S30}$  values at a strong-motion station with an accuracy of approximately +/- 50 m/sec. As the additional validation, correlations are examined between the estimated  $V_{S30}$  and the site classification at the JMA stations, and between the predicted peak ground velocities from the estimated  $V_{S30}$  and the observed ones for Japanese recent major earthquakes. The results indicate the validity of the estimated  $V_{S30}$  values.

**KEYWORDS:** average shear-wave velocity, strong-motion station, JMA, K-NET, KiK-net

### 1. INTRODUCTION

In Japan, nationwide strong-motion seismograph networks, e.g., the K-NET and KiK-net of the National Research Institute for Earth Science and Disaster Prevention (NIED) and the 95-type seismometer network of the Japan Meteorological Agency (JMA) have been operated. Borehole shear-wave velocity logs are available at all of the K-NET and KiK-net stations while the soil condition at the JMA station is not investigated. Therefore, it is difficult to analyze the strong-motion records obtained at the JMA station considering the local site condition. To classify the local site condition, average shear-wave velocity to a certain depth of the ground has been widely used (Borcherdt, 1978). Especially, average shear-wave velocity in the upper 30 meters ( $V_{S30}$ ) is mostly in practical use in classification of surface geological unit which is utilized in the National Seismic Hazard Mapping Project in Japan (Fujiwara et al., 2004) and in U.S. building codes (Borcherdt, 1994).

Value of  $V_{S30}$  at a site can be computed from geotechnical data, such as velocity logging and boring log, or estimated from microtremor array observation (Konno and Kataoka, 2000). However, to obtain these data over a wide area, much time and labor are required because the data necessitate on-site drilling or measurement. The estimate of  $V_{S30}$  can be also obtained from surface geology in the nationwide geomorphologic database in Japan (Fujimoto and Midorikawa, 2004; Matsuoka et al., 2006). Furthermore, Wald and Allen (2007) derived the global  $V_{S30}$  map directly from 30 arc sec topographic data. Since the mesh size used in these studies is about 1km by 1km,  $V_{S30}$  estimates from such mapped geology may differ from actual  $V_{S30}$  at a site.

In this study, we develop a simple method for estimating  $V_{S30}$  at a strong-motion station mainly derived from peak ground motions recorded at a pair of stations located closely each other. By applying the method to the recordings obtained at the K-NET, KiK-net and JMA networks throughout Japan,  $V_{S30}$  values at the JMA strong-motion stations are estimated. To examine the estimation accuracy of the  $V_{S30}$ , predicted  $V_{S30}$  values from the method are compared with those inferred from boring data obtained in the vicinity of the JMA station,

site classification at the JMA station, and seismic ground motion records during recent major earthquakes.

## 2. METHOD AND DATASET

### 2.1. Method

We explain a method for estimating  $V_S30$  at a strong-motion station. As illustrated in Figure 1, for a pair of strong-motion station located closely each other, shear-wave velocity profile is available at one station (“known station”) that is not obtained at another station (“unknown station”). During a certain earthquake, peak ground velocities recorded at known and unknown stations are referred to as  $PGV_k$  and  $PGV_u$ , respectively. Peak amplitude ratio corrected by the reciprocal ratio of hypocentral distances for the station pair provides a relative amplification factor ( $AF'$ ).

$$AF' = (PGV_u/PGV_k)(X_u/X_k) \quad (2.1)$$

where  $X_k$  and  $X_u$  are the distances from an hypocenter to known and unknown stations, respectively. Fujimoto and Midorikawa (2006) showed seismic site amplification factor ( $AF$ ) decreases with an increase in  $V_S30$  with slope  $b$  on average based on the ground motion records and  $V_S30$  measurements at the K-NET and KiK-net. Therefore,  $V_S30$  value at unknown station ( $V_S30_u$ ) can be expressed by Eqn. 2.2.

$$\log V_S30_u = \log V_S30_k + \log AF'/b \quad (2.2)$$

where  $V_S30_k$  is average shear-wave velocity at known station computed from measured shear-wave velocity profile. Thus, we can obtain  $V_S30$  estimate at a strong-motion station not having shear-wave velocity data by substituting  $AF'$ ,  $V_S30_k$ , and  $b$  into Eqn. 2.2.

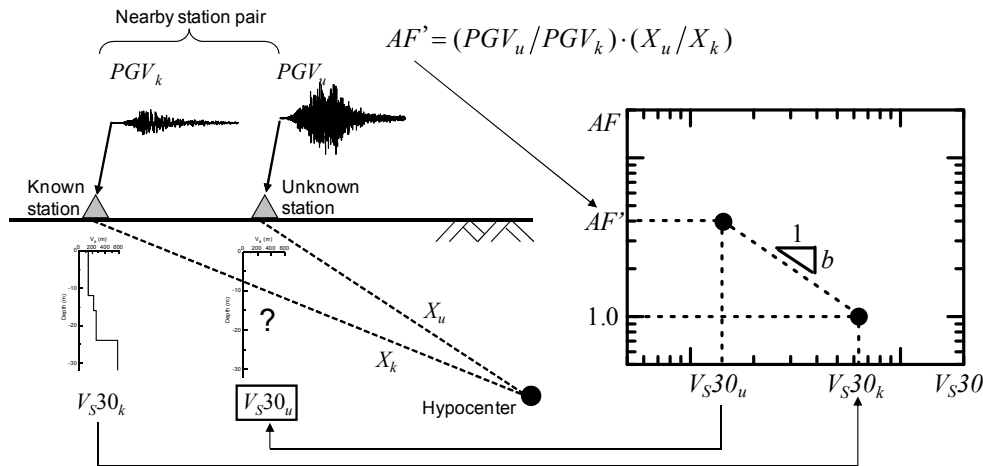


Figure 1 Schematic diagram of prediction method

### 2.2. Dataset

K-NET and KiK-net are the nationwide strong-motion seismograph networks consisted of 1,001 and 495 stations with a spacing of 25 km averagely. Japan Meteorological Agency (JMA) also has nationwide strong-motion network consisted of 602 stations. Combination of these strong-motion networks offers the opportunity to pair nearby strong-motion stations. Borehole shear-wave velocity data is available at all of the K-NET and KiK-net stations however that is not investigated at the JMA station. Thus, we adopt the K-NET and KiK-net stations as the “known station” and the JMA station as the “unknown station” in this study. We can compute  $V_S30$  values at 758 known stations and use these values as  $V_S30_k$ . Figure 2 shows the location of the K-NET and KiK-net stations (known station) by closed circles.

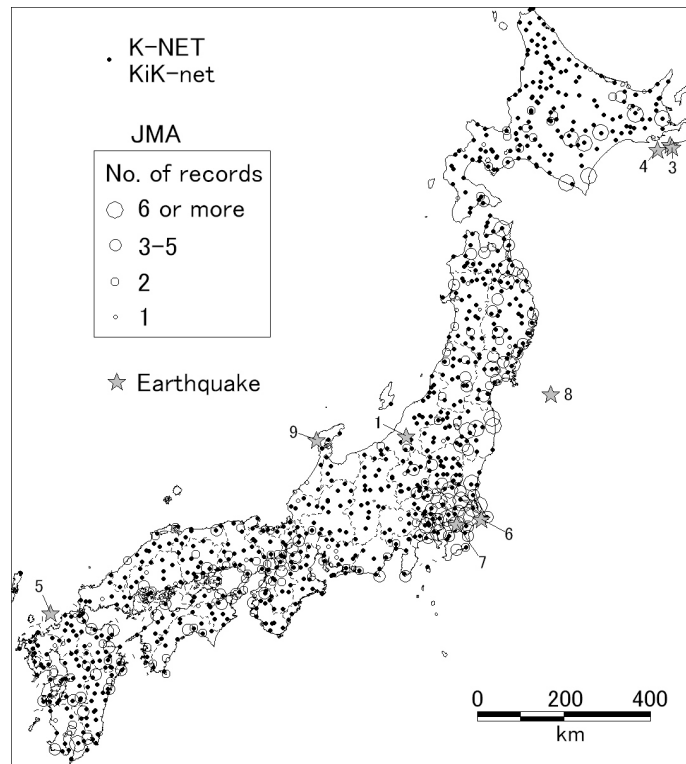


Figure 2 Location of K-NET, KiK-net and JMA stations

To pair the JMA station (unknown station) with the K-NET or KiK-net stations (known stations), station-to-station distances between the JMA station and both the K-NET and KiK-net stations are calculated, and then each JMA station is paired with one of the nearest K-NET or KiK-net station. Since the propagation path effect is considered to be not negligible for station distance greater than about 30 km (Borcherdt, 2002), the station pair with station distance of more than 30 km are excluded. Consequently, 339 known-unknown station pairs are made. For the station pairs, ground motion records of the earthquakes occurred up until December, 2003 with peak ground accelerations of less than 100 gals are collected. Common recordings obtained at both the known and unknown stations are necessary to compute  $AF^2$  value however such records are not available at 57 station pairs. Therefore, 282 station pairs are used in the subsequent analysis. The location of the paired JMA stations is shown by open circles in Figure 2.

A histogram showing the number of common recordings obtained at a total of 282 known-unknown pairs is shown in Figure 3. Station pairs with common records less than 2 and 5 earthquakes account for about 40% and 80% of the total pairs, respectively. Figure 4 shows the histogram of the distance between the known and unknown stations. The number of station pairs tends to increase as the station pair distance becomes shorter. Station pair distance less than 5 km makes up about 30% of the total pairs.

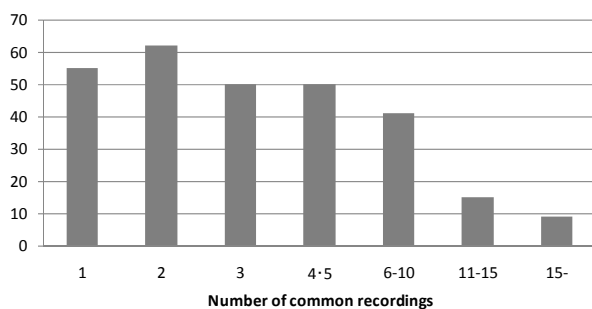


Figure 3 Histogram of number of common records

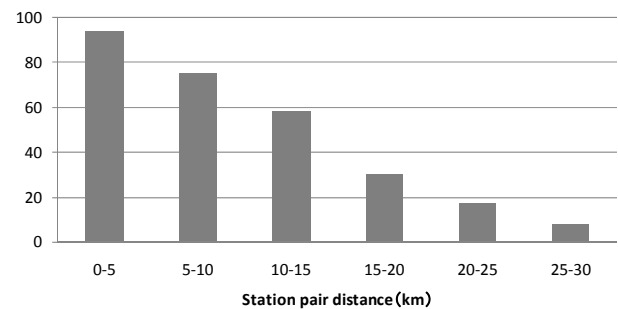


Figure 4 Histogram of station pair distance

### 3. ESTIMATES OF $V_{S30}$ AT JMA STATIONS

For the 282 known-unknown station pairs, relative amplification factors ( $AF'$ ) are calculated by substituting peak ground velocities ( $PGV$ ) and hypocentral distances into Eqn. 2.1. The  $PGV$  is adopted as the ground motion parameter in Eqn. 2.1 because this parameter shows better correlation with  $V_{S30}$  than does  $PGA$  (Fujimoto and Midorikawa, 2006). Value of  $AF'$  is defined as the largest value of the corresponding quantity computed from the two horizontal components obtained at each station pair. Substituting the  $AF'$  together with average shear-wave velocity at known station ( $V_{S30_k}$ ) and average value of slope  $b$  specified as  $-0.852$  (Fujimoto and Midorikawa, 2006) into Eqn. 2.2, we obtain the  $V_{S30}$  estimate at the JMA stations.

Figure 5 shows the correlation between the estimated  $V_{S30}$  and magnitude ( $M$ ) for each paired JMA station. The estimated  $V_{S30}$  remains relatively constant at most of the stations however a large scatter of the  $V_{S30}$  is found at the paired station with the recordings from the earthquake of magnitudes 5.0 or less, e.g., the JMA Urakawa [D62], Kuki [51E] and Yonago [EA0]. The  $PGV$  which is used to compute the  $AF'$  correlates better with ground motion over a mid-period range (0.5-2.0 sec) (Kobayashi and Nagahashi, 1973), however mid-period motions are less dominant in the records from the earthquakes with smaller magnitude than are short-period motion. Therefore, the variance of  $AF'$  may increase as magnitude of the earthquake becomes smaller. Consequently, Value of  $V_{S30_u}$  are estimated by substituting the  $AF'$  computed from records with  $M > 5.0$  into Eqn. 2.2.

Figure 6 shows the distribution of predicted  $V_{S30}$  values at 261 JMA stations. For reference, average  $V_{S30}$  values computed from the records with  $M > 5.0$  are shown by dotted line in Figure 5. As shown in Figure 6, many of low  $V_{S30}$  stations are located on alluvial plain such as Kanto and Osaka Plains. Figure 7 presents the histogram of  $V_{S30}$  estimates. Predicted  $V_{S30}$  reaches a peak around 200 m/sec, ranging widely from 100 m/sec of very soft soil to more than 600 m/sec of engineering bedrock.

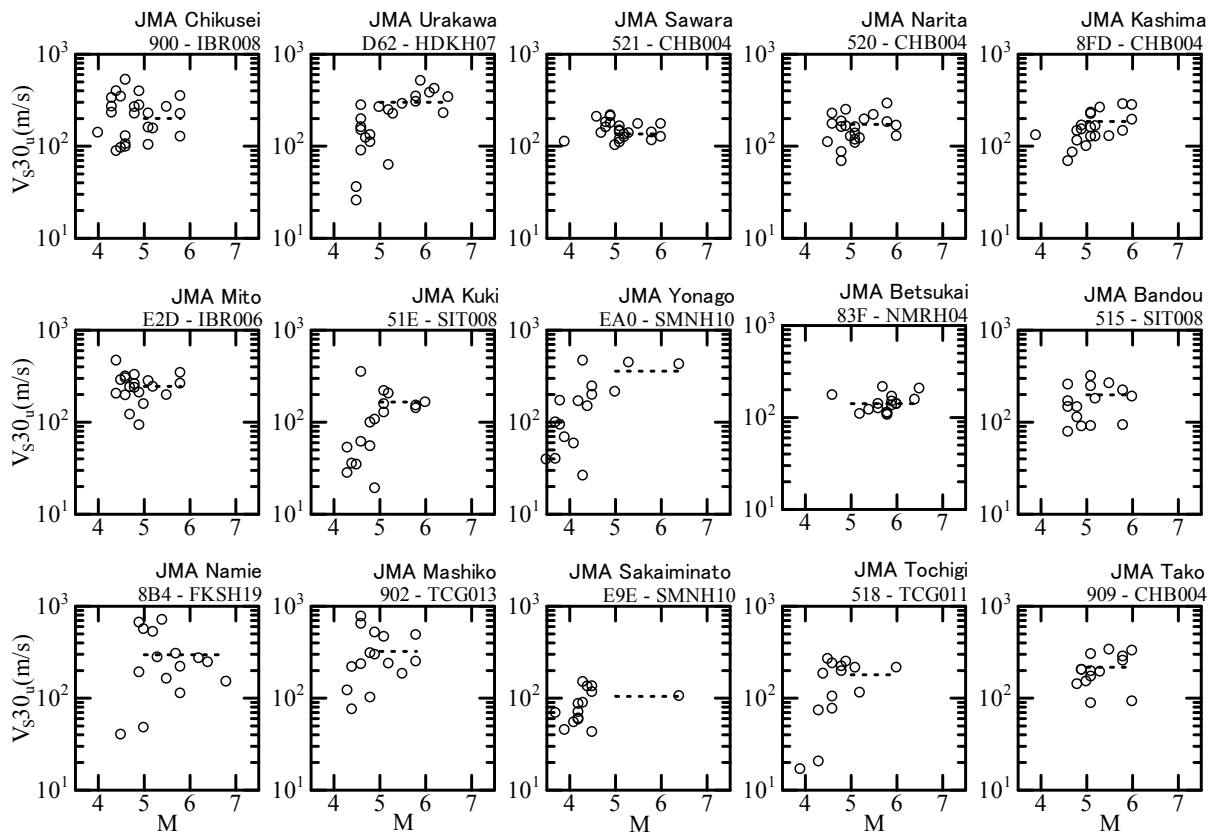


Figure 5 Correlation between  $V_{S30}$  and magnitude

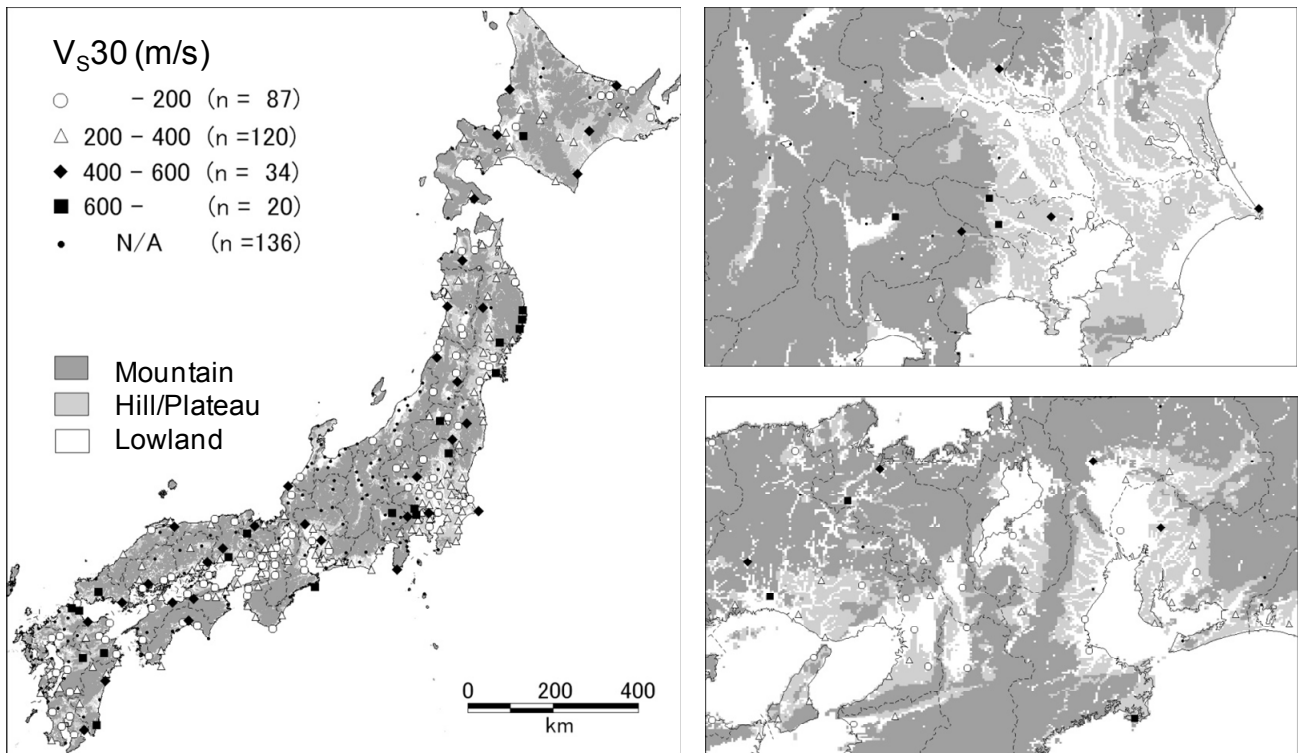


Figure 6 Distribution of  $V_{s30}$  estimate at JMA stations  
 (left: national map, upper right: Kanto area map, lower right: Hanshin-Chukyo area map)

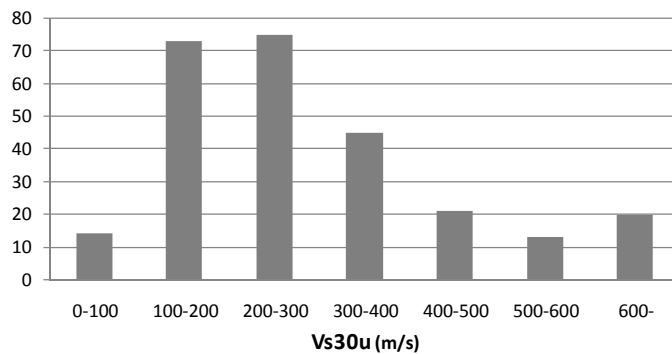


Figure 7 Histogram of  $V_{s30}$  estimate at JMA stations

#### 4. COMPARISON BETWEEN ESTIMATED AND OBSERVED $V_{s30}$

To examine the estimation accuracy of  $V_{s30}$ , boring logs with SPT N-value obtained in the vicinity of the JMA stations are compiled from several sources. We use 13 boring data that satisfies the following conditions: 1) drilling depth is 30 meters or more, 2) distance between the JMA station and borehole site is within 200 meters, 3) both the JMA station and borehole site are located on the same geomorphological unit.  $V_{s30}$  values at the 13 boring sites near the JMA station are computed based on the shear-wave velocity model estimated from N-value and depth using the empirical equation (Ohta and Goto, 1978). Figure 8 shows a comparison of the  $V_{s30}$  between the values predicted from the station-pair method and those estimated from adjacent boring data. The agreement between the predicted and estimated  $V_{s30}$  is excellent. This result indicates that the method developed herein can predict the  $V_{s30}$  at a strong-motion station with an accuracy of approximately  $\pm 50$  m/sec.

To examine the applicability of the station-pair method for velocity range more than 300 m/sec, we compare the predicted  $V_{s30}$  with site classifications at each JMA station. Site class at the JMA station was investigated (Yoshida and Katsumata, 1972), and each station was classified into four categories: 1) rock, 2) stiff soil, 3) soft soil, and 4) very soft soil. Figure 9 shows the histogram of the  $V_{s30}$  for each site class. There appears to be a significant shift toward higher velocities as the site class becomes stiffer however relatively low velocities of less than 400 m/sec are seen at rock site. Several of the low  $V_{s30}$  sites are located on weathered rock. Thus, underestimate of  $V_{s30}$  at rock site may come from the overestimation of  $AF'$  due to the ground motion amplification from the low-velocity weathered layer.

To provide more rigorous validation for the station-pair method, we compare the predicted peak ground velocities with observations during recent large earthquakes. We compute peak ground velocity (PGV) at the JMA station by multiplying the seismic site amplification converted from the estimated  $V_{s30}$  using empirical equation (Fujimoto and Midorikawa, 2006) and the peak velocity on engineering bedrock predicted from attenuation relationship (Midorikawa and Ohtake, 2004). Correlation between the predicted and observed PGV at the JMA station is shown by closed circle in Figure 10. Likewise, the correlations for the K-NET and KiK-net stations are presented by open square and open triangle, respectively. There is a good agreement between the predicted and observed PGV however the predicted values are underestimated for several earthquakes such as Eq. 2, 3, 4, and 8. As shown in Figure 2, these earthquakes were occurred in the north-east part of Japan, where the anomalous seismic intensity of subduction zone has been observed. This probably affects that the observed PGV show higher value compared to predicted one. Figure 11 shows the logarithmic standard deviations for the ratio of predicted and observed PGV. The standard deviation of the JMA station (closed circle) ranges 0.2-0.3, that is almost the same with those of the K-NET (open rectangle) and KiK-net (open triangle).

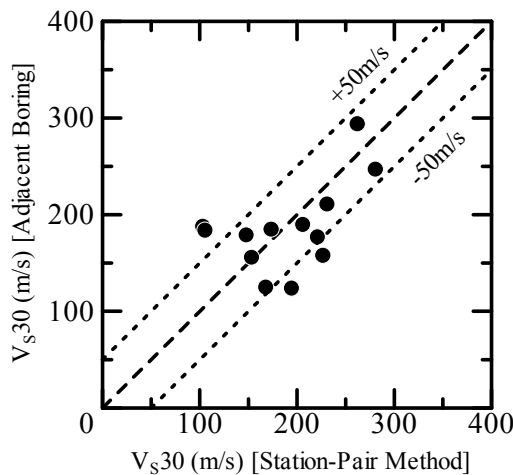


Figure 8 Comparison of  $V_{s30}$

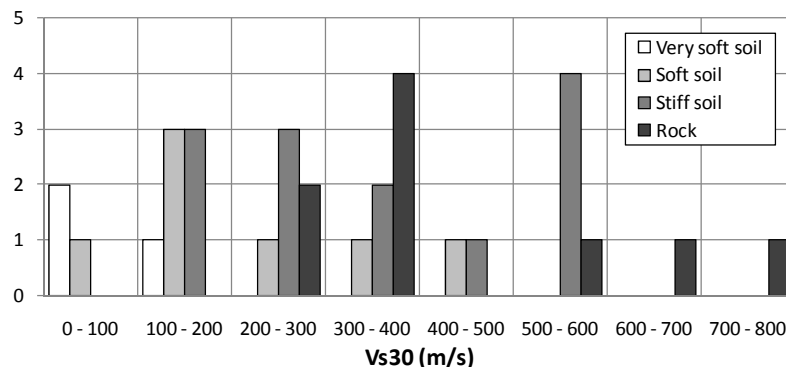


Figure 9 Histogram of  $V_S30$  for each site class

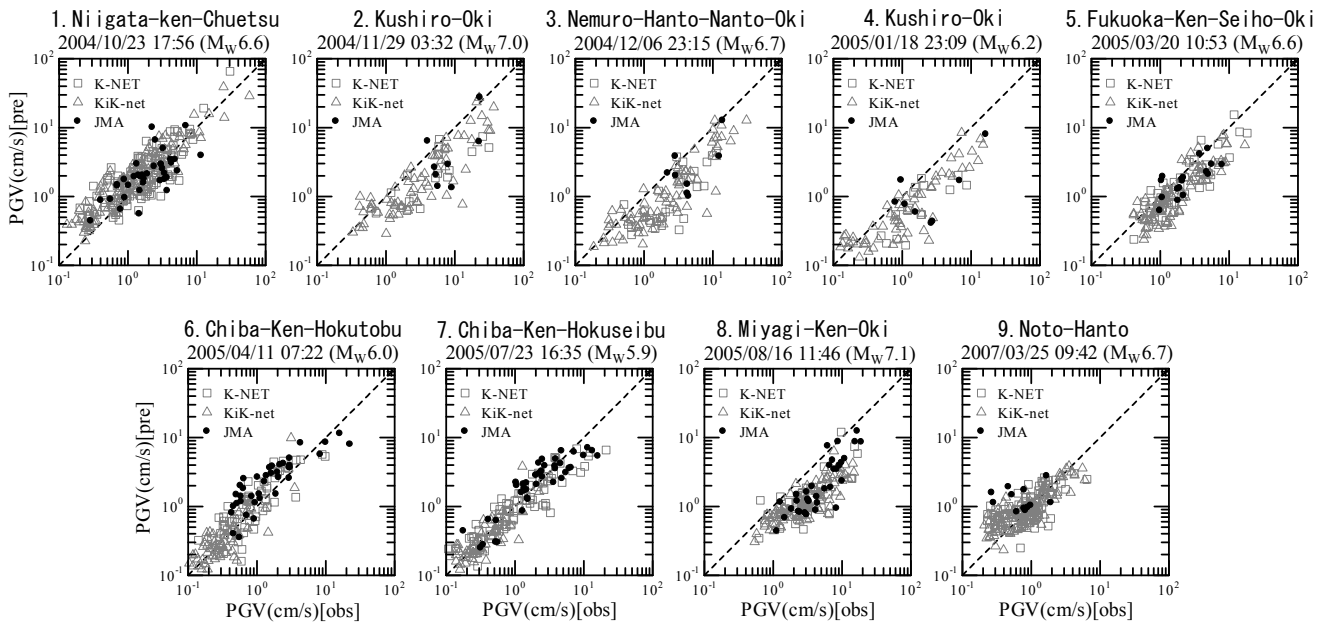


Figure 10 Comparison of PGV

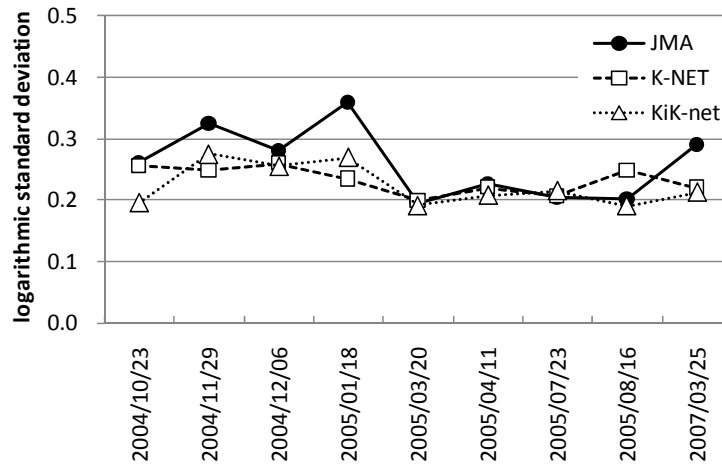


Figure 11 Comparison of logarithmic standard deviation

## 5. CONCLUSIONS

We develop a simple method for estimating average shear-wave velocity in the upper 30 meters of the ground ( $V_S30$ ) at a strong-motion station by using recorded motions at a pair of stations located closely each other. For the station pair, an estimate of  $V_S30$  at one of the stations where the soil condition is unknown is derived mainly from  $V_S30$  at another station where the shear-wave velocity data is available and relative amplification factor between the stations. By applying this method to the ground motion records of the JMA, K-NET and KiK-net strong-motion networks in Japan, the  $V_S30$  values are estimated at JMA stations. The estimated  $V_S30$  remains relatively constant at most of the stations however a large scatter of  $V_S30$  are found in some cases when using the recorded motions of magnitudes 5.0 or less. Therefore, using only the records of magnitude more than 5.0, the  $V_S30$  values are recalculated at the 261 JMA stations throughout Japan.

The  $V_{s30}$  estimated in this study are compared with those inferred from boring data obtained in the vicinity of the JMA station. The result indicates that the method proposed in this study can predict the  $V_{s30}$  values at a strong-motion station with an accuracy of approximately +/- 50 m/sec. Relationship between  $V_{s30}$  and four site classes such as rock, stiff soil, soft soil and very soft soil at each JMA station are examined. The results shows that there appears to be a significant shift toward higher velocities as the site class becomes stiffer. By multiplying seismic site amplification factors converted from the  $V_{s30}$  estimated in this study and peak velocities on engineering bedrock predicted from attenuation relationship, peak ground velocities are computed. Compared with observed peak ground velocities for recent major nine earthquakes occurred in Japan, the computations show good agreement with observations.

## REFERENCES

- Borcherdt, R.D., Gibbs, J.F., and Fumal, T.E. (1978). Progress on ground motion predictions for the San Francisco Bay region, California, *Proc. of the 2nd International Conf. on Microzonation*, **1**, 241-253.
- Borcherdt, R.D. (1994). Estimates of site-dependent response spectra for design (Methodology and Justification), *Earthquake Spectra*, **10**, 617-653.
- Borcherdt, R.D. (2002). Empirical evidence for acceleration-dependent amplification factors, *Bull. Seism. Soc. Am.*, **82:2**, 603-641.
- Fujimoto, K. and Midorikawa, S. (2004). Prediction of average shear-wave velocity for ground shaking mapping using the Digital National Land Information of Japan, *Proc. of the 13th World Conf. on Earthquake Engineering*, Paper No.1107.
- Fujimoto, K. and Midorikawa, S. (2006). Empirical estimates of site amplification factor from strong-motion records at nearby station pairs, *Proc. of the 1st European Conf. on Earthquake Engineering and Seismology*, ID No. 251.
- Fujiwara, H., Aoi, S., Kawai, S., Senna, S., Ishii, T., Okumura, T., and Hayakawa, Y. (2004). Outline of strong-motion evaluation in National Seismic Hazard Mapping Project of Japan, *Journal of Japan Association for Earthquake Engineering*, **4:3**, 50-61.
- Kobayashi, H. and Nagahashi, S. (1973). Evaluation of earthquake effects on the deformation of multi-storied buildings by ground motion amplitudes, *Trans of A.I.J.*, 210, 11-22. (in Japanese with English abstract)
- Konno, K. and Kataoka, S. (2000). New Method for Estimating The Average S-Wave Velocity of The Ground, *Proc. of the 6th International Conf. on Seismic Zonation*.
- Matsuoka, M., Wakamatsu, K., Fujimoto, K., and Midorikawa, S. (2006). Average Shear-wave Velocity Mapping Using Japan Engineering Geomorphologic Classification Map, *Journal of Structural Engineering and Earthquake Engineering, Japan Society of Civil Engineers*, **23:1**, 57s-68s.
- Midorikawa, S. and Ohtake, Y. (2004). Variance of peak ground acceleration and velocity in attenuation relationships, *Proc. of the 13th World Conf. on Earthquake Engineering*, Paper No.325.
- Ohta, Y. and Goto, N. (1978). Physical background of the statistically obtained S wave velocity equation in terms of soil indexes, *Butsuri-Tanko (Geophysical Exploration)*, **31:1**, 8-17. (in Japanese with English abstract)
- Yoshida, H. and Katsumata, M. (1972). Ground conditions of seismological stations in J.M.A. network, *Quarterly journal of seismology*, **37:3**, pp.113-115. (in Japanese)
- Wald, D.J. and Allen, T.I. (2007). Topographic slope as a proxy for seismic site conditions and amplification, *Bull. Seism. Soc. Am.*, **97:5**, 1379-1395.