von Neumann's inequality for contractions

Paramita Pramanick

Abstract

The von Neumann's inequality states that if T is a contraction on a complex Hilbert space \mathcal{H} then for any polynomial p,

$$||p(T)|| \le ||p||_{\infty},$$

where $||p||_{\infty} = \sup_{|z| \le 1} |p(z)|$. In this talk, we will present an elementrary proof of this inequality.